### Carbon dating: When is it beneficial to link ETSs?

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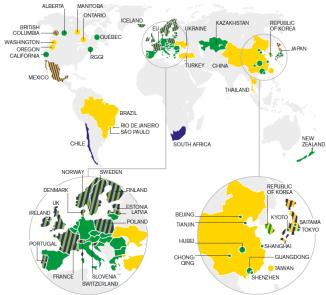
Chaire Economie du Climat, Paris 30 October 2015







Figure 1 Overview of existing, emerging, and potential regional, national, and subnational carbon pricing instruments (ETS and tax)



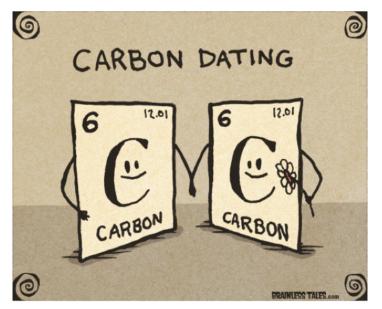
Source: World Bank (2015)

"The ability to link regional, national, and sub-national climate policies will be essential to enhancing the cost-effectiveness of such a system [emerging post COP21]— and thus the likelihood of achieving significant global emissions reductions." **Stavins (2015)** 

"Linking the EU ETS with other cap-and-trade systems offers several potential benefits, including reducing the cost of cutting emissions, increasing market liquidity, making the carbon price more stable, leveling the international playing field and supporting global cooperation on climate change." European Commission (2015)

"The Agreement [in COP21] should support countries interested in using international market linkages to achieve more ambitious emissions reductions. Networked carbon markets perform better, environmentally and economically, enabling nations and businesses to better manage the transition to a cleaner economy" IETA (2015)

#### Looking for a carbon date...?



#### Overview

Evaluate economic advantage of linking over autarky

$$E[\Delta] = E[\delta_1] + E[\delta_2]$$

as a function of pair characteristics

$$\{(\psi_1,\sigma_1),(\psi_2,\sigma_2),\rho\}$$

where  $\psi_i = size$ ,  $\sigma_i = variability$  and  $\rho = correlation$ 

- Covariance matrix of shocks and ETS sizes are crucial
- Unilateral distortions matter (if sufficient time)

- Calibrate pair-characteristics to country emissions data over 1950-2012
- Substantial empirical variation in  $E[\Delta]$  and  $E[\delta_i]$

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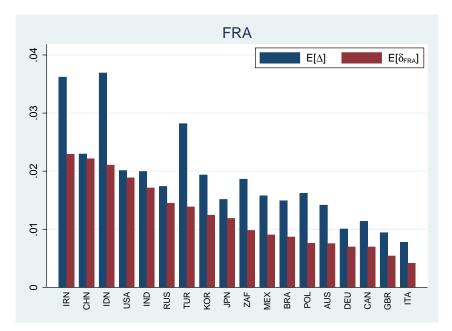
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## Two-country model (i = 1, 2)

#### Benefits of emissions

$$B_i(q_i,\theta_i) = b_0 + (b_1 + \theta_i)q_i - \frac{b_2}{2\psi_i}q_i^2$$

Shocks: e.g. business cycles, energy prices, weather, etc.

$$\mathbb{E}( heta_i)=0$$
 
$$\mathbb{V}( heta_i)=\sigma_i^2\geq 0 \qquad \qquad \textit{Corr}( heta_1, heta_2)=
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Damages from emissions

$$D_i(q_1+q_2) = d_0+d_1(q_1+q_2)+\frac{d_2}{2}(q_1+q_2)^2$$

#### Assume

- i) identical countries except in  $\psi_i$  and  $\sigma$
- ii) same (second best) quotas under both autarky and linking

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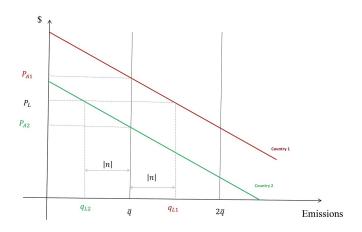
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# Interior autarky & linking equilibria $(\psi_1=\psi_2)$



- \* Autarky prices  $p_{Ai}$  depend on own shock
- \* Linking price  $p_L$  depends on average shock with  $n=rac{ heta_2- heta_1}{2b_2}$
- \* Define IAE when  $p_{Ai} > 0$  and ILE when  $n \in (-\bar{q}, \bar{q})$

Doda & Taschini (2015)

## Economic advantage of linking over autarky

Country-specific advantage of linking

$$\tilde{\delta}_{i} = [B_{i}(q_{Li}, \theta_{i}) - p_{L}q_{Li} - D_{i}(q_{L1} + q_{L2}) + p_{L}\bar{q}_{i} - \psi_{i}\varepsilon] 
- [B_{i}(q_{Ai}, \theta_{i}) - p_{Ai}q_{Ai} - D_{i}(q_{A1} + q_{A2}) + p_{Ai}\bar{q}_{Ai}]$$

$$\begin{array}{rcl} \delta_{1} & = & B_{1}(\bar{q}_{1}-n,\theta_{1}) - B_{1}(\bar{q}_{1},\theta_{1}) + \rho_{L}n - \psi_{1}\varepsilon \\ \delta_{2} & = & B_{2}(\bar{q}_{2}+n,\theta_{2}) - B_{2}(\bar{q}_{2},\theta_{2}) - \rho_{L}n - \psi_{2}\varepsilon \\ \Delta & = & \delta_{1} + \delta_{2} \end{array}$$

$$n = \frac{1}{b_2} \frac{\psi_1 \psi_2}{(\psi_1 + \psi_2)} (\theta_2 - \theta_1)$$

**Remark:** Sunk cost are independent of  $\{\sigma_1^2, \sigma_2^2, \rho\}$ 

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In interior equilibria

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### Analytical results: Decomposing economic advantage

#### Proposition

Fix pair characteristics  $\{(\psi_1, \sigma_1), (\psi_2, \sigma_2), \rho\}$  and let  $\varepsilon \geq 0$ . Define pair size effect (PSE), volatility effect (VE) and dependence effect (DE) as

$$\begin{array}{ccc} \textit{PSE}(\psi_1, \psi_2) & \equiv & \frac{\psi_1 \psi_2}{2 \, b_2 \, (\psi_1 + \psi_2)} \\ \\ \textit{VE}(\sigma_1, \sigma_2) & \equiv & \sigma_1^2 + \sigma_2^2 \\ \textit{DE}(\sigma_1, \sigma_2, \rho) & \equiv & -2 \sigma_1 \sigma_2 \rho \end{array}$$

Then in interior equilibria

$$E[\Delta] = PSE(VE + DE) - (\psi_1 + \psi_2) \varepsilon$$

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### 1) Calibrate $\psi_i$ to observed $CO_2$ emissions in 2012

Assume in each country i

- No climate change policy
- Identical technologies
- $\theta_i = E[\theta_i] = 0$

$$\psi_i = \frac{b_2}{b_1} q_{i,2012}$$

2) Calibrate  $\{\sigma_i, \sigma_i, \rho\}$  using HP decomposition of  $e_{it}$ 

$$\sigma(\theta_i) = \frac{b_2}{\psi_i} \sigma(e_{it}^c)$$
  $\rho(\theta_i, \theta_j) = Corr(e_{it}^c, e_{jt}^c)$ 

- 3) Data on  $e_{it}$  for top 20 emitters for 1950-2012
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### Empirical results: Overview

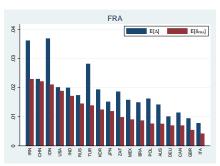
		190 pa	irs incl. SA	vO	171 pairs excl. SAU			
	mean	sdev	min	max	mean	sdev	min	max
Ε[Δ]	0.042	0.079	0.001	0.438	0.018	0.013	0.001	0.061
			RUS-USA	CHN-SAU			RUS-USA	CHN-IDN
PSE	0.038	0.033	0.017	0.355	0.039	0.035	0.017	0.355
VE	1.527	2.585	0.008	10.064	0.682	0.480	0.008	2.159
DE	- 0.084	0.254	-2.153	0.560	-0.056	0.112	-0.520	0.439

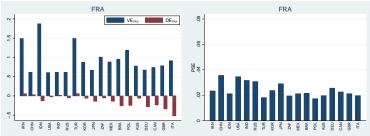
Note: Summary statistics for  $\sigma(e^c_{it})$  and  $Corr(e^c_{it}, e^c_{jt})$ 

Doda & Taschini (2015)

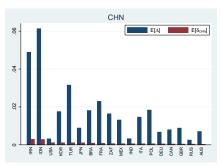
Carbon Dating

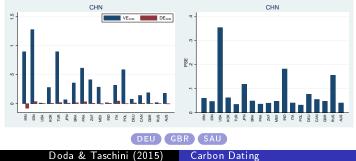
### Empirical results: France





### Empirical results: China





### Analytical results: Unilateral tax distortions

#### Proposition

Maintain the conditions in Proposition 1 but assume  $\psi_1 = \psi_2 = 1$ . Let  $\delta_i(\tau^{\times}, \tau^m)$  denote the economic advantage of linking in country i = 1, 2 when country 1 unilaterally imposes  $(\tau^{\times}, \tau^m)$ . Then in interior equilibria  $\exists (\bar{\tau}^{\times}, \bar{\tau}^m) \in \mathbb{R}^2_{++}$  such that

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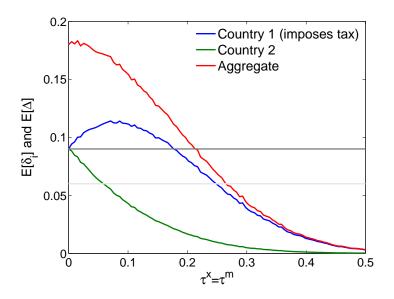
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#### Numerical illustration: Unilateral tax distortions



#### Conclusions

- You want your partner to be large, volatile and negatively correlated
- Much variation in the data to make the exercise worthwhile
- Sunk costs and unilateral distortions can kill a carbon date
- Linking can be a responsiveness mechanism

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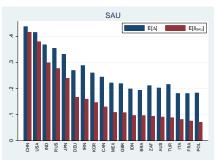
(GRI Working Paper No.208)

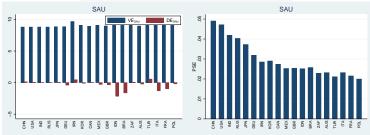
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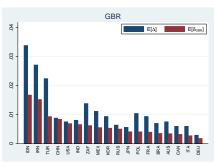
THANK YOU!

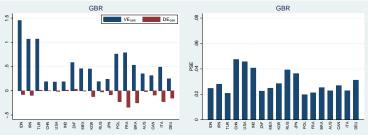
### Empirical results: UK



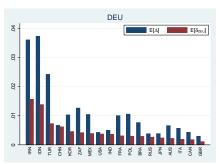


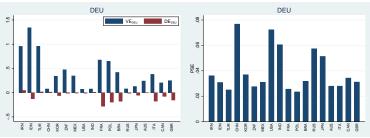
# Empirical results: UK





### Empirical results: Germany





### Empirical results: Observed fluctations in emissions

Table: Summary statistics:  $\sigma(e_{it}^c)$  and  $Corr(e_{it}^c, e_{jt}^c)$ 

	mean	sdev	min	max	N
$\psi_i$	0.142	0.234	0.033	1	20
ΨΙ			POL	CHN	
$\sigma(e^c_{it})$	0.038	0.032	0.017 AUS	0.153 SAU	20
$Corr(e_{it}^c, e_{jt}^c)$	0.122	0.218	-0.459 CHN- ITA	0.688 DEU-FRA	190

Doda & Taschini (2015)

Carbon Dating