

# Essays on Spatial and Temporal Interconnections between and within Emissions Trading Systems

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# Emissions trading as a pivotal climate policy tool?

- Emissions trading is a well-established instrument to curb GHG emissions
  - track record of ETS implementation in 19 jurisdictions (ICAP, 2017)
  - 7 GtCO<sub>2</sub>e or 13% of worldwide GHG emissions (World Bank, 2017)



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- Thus far linkages remain few and far between and some systems (e.g. EUETS) are criticized for not delivering adequate price signals
- ▶ Focus on spatial and temporal interconnections between and within ETSs

# Research questions and presentation outline

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- Contributions, Perspectives & Conclusions

## CHAPTER 1

### Transitional Restricted Bilateral Linkages between ETSs

In collaboration with Christian de Perthuis (Paris-Dauphine)  
Submitted to *Environmental & Resource Economics*  
Available as a FAERE policy paper and CEC working paper

# Gradual linkage approach with trade restrictions

- A link could be approached gradually (Jaffe et al., 2009). Two options:
  - indirect linkages e.g. through the CDM:  $EU \leftrightarrow CDM \leftrightarrow NZ$
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- Some bilateral linkages have been initiated through unilateral trading
  - Norway-EUETS, Aviation-EUETS, Australia-EUETS
- Effects of trade restrictions often studied with modelling exercises
  - esp. during Kyoto era (special issue in EJ), Ellerman & Sue Wing (2000), Rehdanz & Tol (2005), Burtraw et al. (2013), Gavard et al. (2016)

# A unifying framework to compare linkage restrictions

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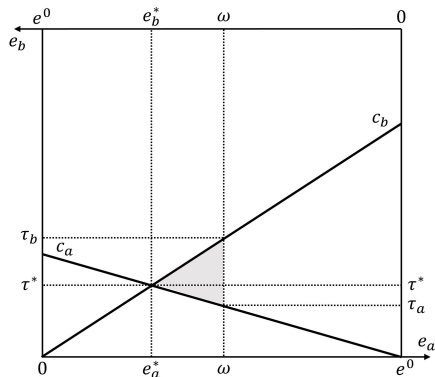
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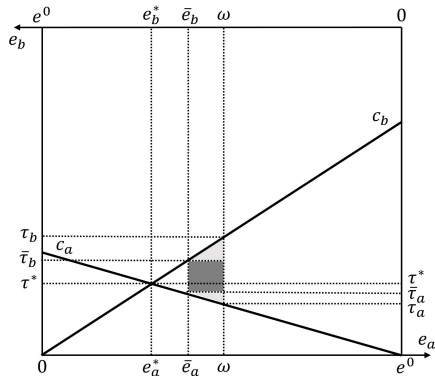
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  - sufficient to pinpoint key differences between alternative restrictions
- Emission caps are exogenous and fixed once and for all
  - domestic caps result from complex negotiations (Flachsland et al., 2009)

# Comparative effects of alternative link restrictions



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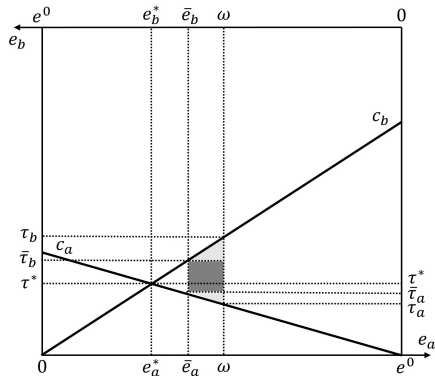
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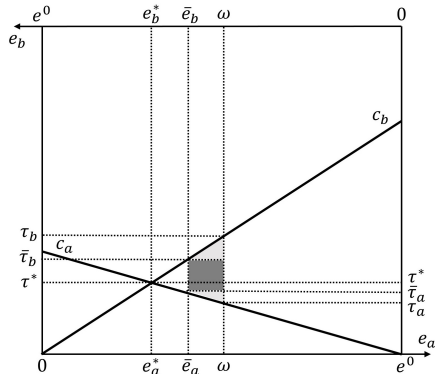


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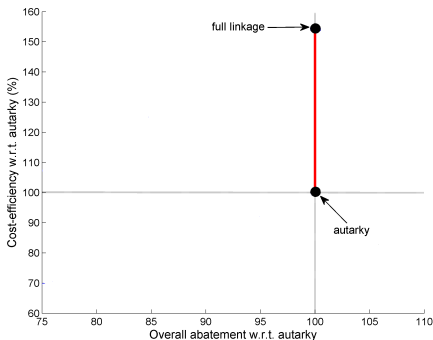
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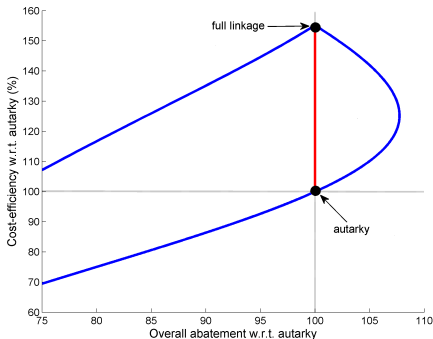
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- Effects of exchange rates are more subtle: abatements are not fungible
  - correct for relative stringency & potential to increase ambition
  - outcomes can be worse than QR&BT or autarky: challenging to select/update

## CHAPTER 2

### Multilateral Linkages between ETSs under Uncertainty

In collaboration with Baran Doda & Luca Taschini (LSE)

Target journal: *Journal of Public Economics*

Available as a GRI working paper and CEC working paper

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- Emission caps are exogenous and fixed once and for all
  - no strategic interactions: diverge from IEA literature, e.g. Helm (2003)

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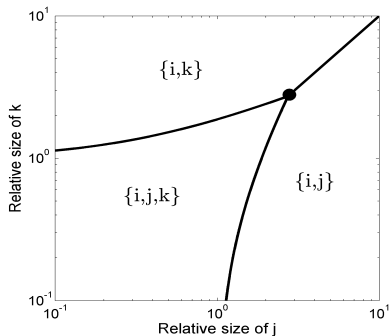
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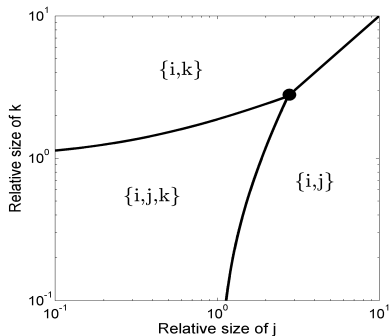
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- Linkage gains arising due to uncertainty are often underappreciated
  - preferences across bilateral links: a jurisdiction prefers large partners whose permit demands are volatile and weakly correlated

# Gains and preferences in multilaterally linked ETSs



- 3-country world:  $i$  (ref),  $j$  and  $k$

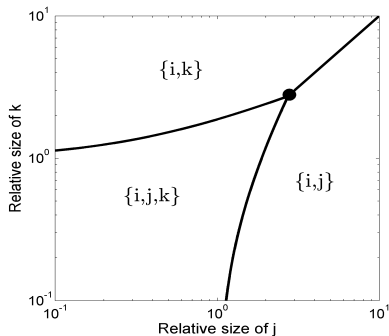
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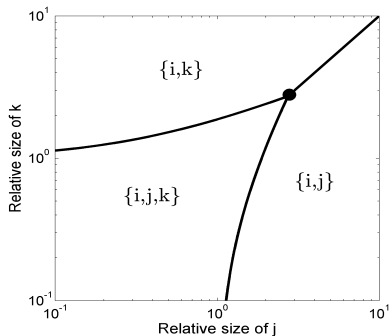


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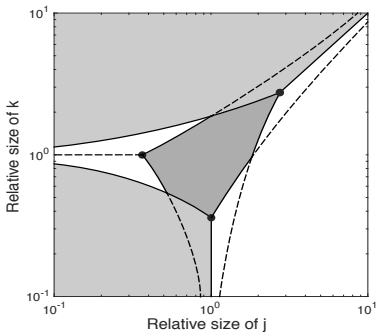
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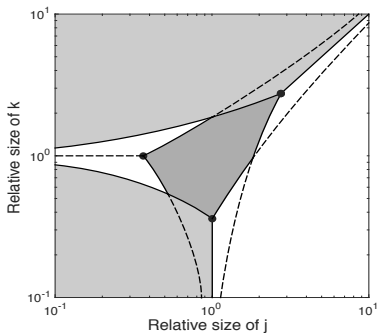
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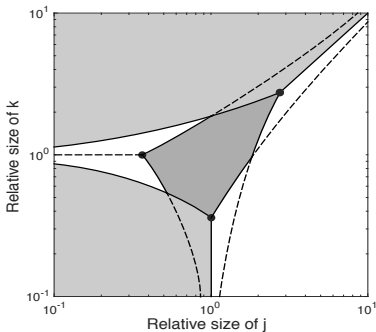
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  - without transfers, jurisdictional linkage preferences do *not* tally
- Calibration to historical emissions data provides some empirical validity
  - CHN prefers {CHN,USA,EUR} but USA/EUR prefer a bilateral link with CHN

## CHAPTER 3

### Intertemporal Abatement Decisions under Ambiguity Aversion

Single-authored article

Target journal: *Journal of Environmental Economics & Management*

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- First attempt to introduce ambiguity aversion in ETS modelling

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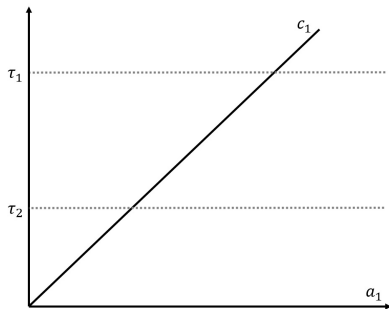
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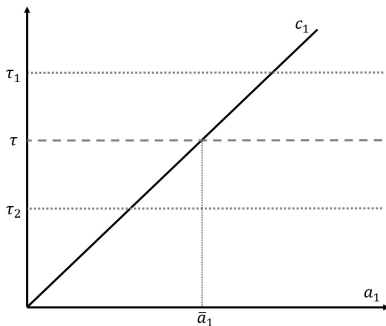
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  - AN-firm abates up to the discounted expected price: intertemporal efficiency obtains with rational expectations (Samuelson, 1971; Schennach, 2000)

# Effects of ambiguity aversion on early abatement decisions



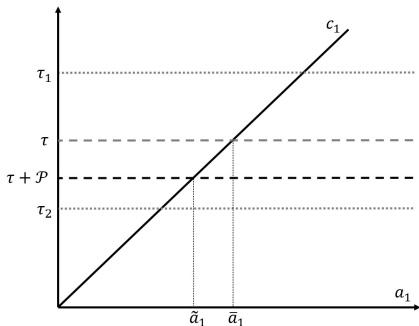
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# Effects of ambiguity aversion on early abatement decisions



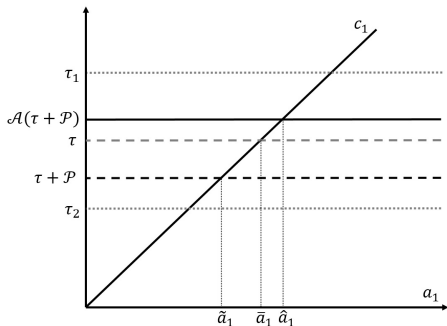
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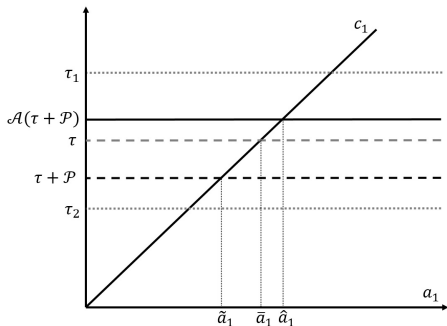
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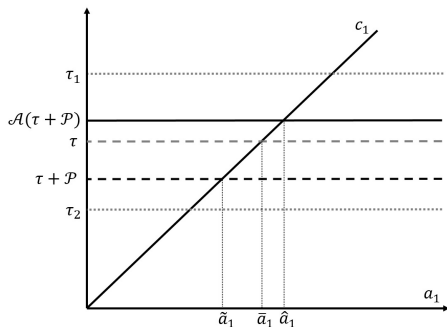
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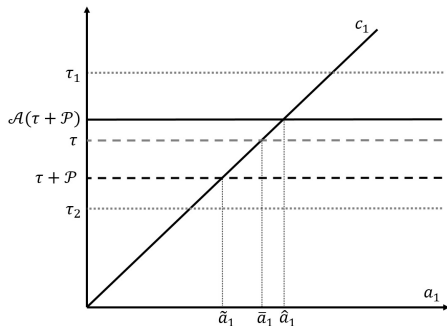
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- Forwards contracts cannot restore intertemporal efficiency

## Contributions, Perspectives & Conclusions

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- Effects of spatial and temporal flexibilities are intertwined
  - can linkage be an instrument to reduce regulatory uncertainty/ambiguity?
  - ETSs are never pure quantity instruments: *linkability* issues
  - significantly linked systems are a long way off: remain a distant dream?
    - political rhetoric around linkage to create an image of 'grand efforts'

**Thank you for your attention**



# Appendices & Discussion

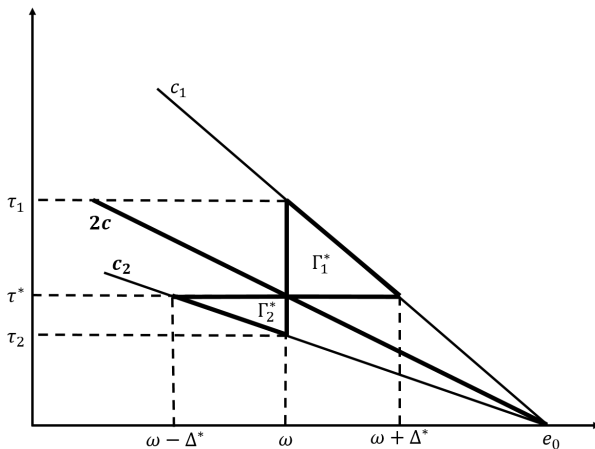
Chapter One

Chapter Two

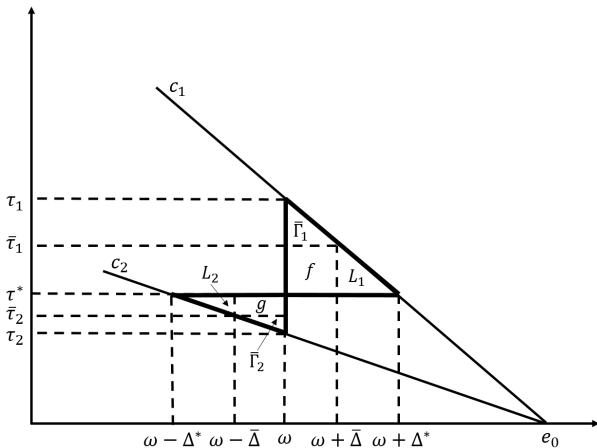
Chapter Three

# Appendix of Chapter 1

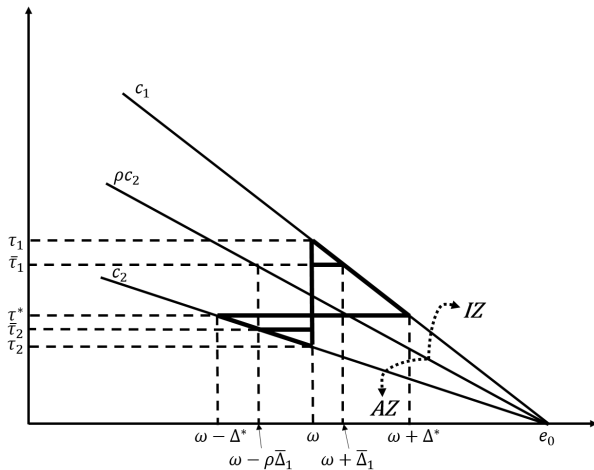
# Autarky and full linkage



# Quantitative restrictions and border taxes



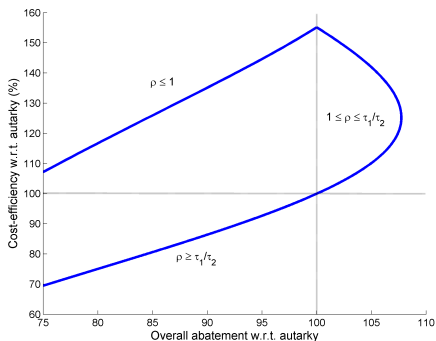
# Exchange rates



# Numerical simulations and indexes

$$I^A = \frac{2\bar{e} - (2\omega + (1 - \rho)\Delta_1(\rho))}{2(\bar{e} - \omega)} = 1 + \frac{(\rho - 1)\Delta_1(\rho)}{2(\bar{e} - \omega)}$$

$$I^{CE} = \ln\left(\frac{C'_1(\bar{e} - \omega)}{C'_2(\bar{e} - \omega)} + 1\right) / \ln\left(\frac{\max_i C'_i(\bar{e} - \omega - \Delta_i(\rho))}{\min_i C'_i(\bar{e} - \omega - \Delta_i(\rho))} + 1\right)$$



## Appendix of Chapter 2

# Two sources of gains from bilateral linkage

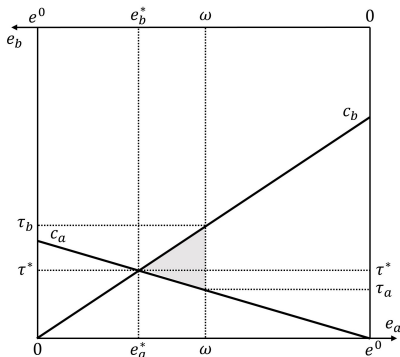


Figure: Certainty (ambition)

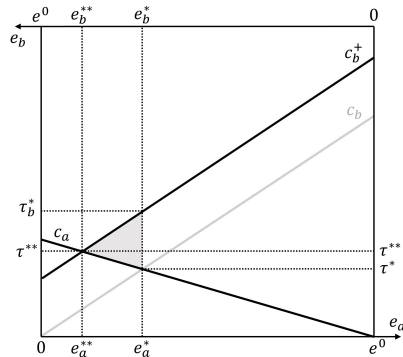


Figure: With (+) shock in country  $b$



# Modelling framework

- $\mathcal{I} = \{1, \dots, n\}$ :  $n$  jurisdictions with independent regulatory authorities
- Benefits of emissions  $q_i \geq 0$  in jurisdiction  $i \in \mathcal{I}$

$$B_i(q_i; \theta_i) = (b_1 + \theta_i)q_i - \frac{b_2}{2\psi_i}q_i^2, \text{ with } b_1, b_2 > 0.$$

Size  $\psi_i$ : measures the volume of  $i$ 's regulated emissions

Shocks  $\theta_i$ : business cycles, energy prices, weather, etc

$$\mathbb{E}\{\theta_i\} = 0, \quad \mathbb{V}\{\theta_i\} = \sigma_i^2, \quad \text{and} \quad \text{Cov}\{\theta_i, \theta_j\} = \rho_{ij}\sigma_i\sigma_j.$$

- Caps are exogenous, fixed once-and-for-all, and proportional to size

$$\omega_i = A \cdot \psi_i, \text{ for all } i \in \mathcal{I}.$$

# Bilateral linkage equilibria

- An  $\{i, j\}$ -linkage equilibrium is a triple  $(p_{\{i,j\}}, q_{\{i,j\},i}, q_{\{i,j\},j})$  where

$$p_{\{i,j\}} = \frac{\psi_i \bar{p}_i + \psi_j \bar{p}_j}{\psi_i + \psi_j}, \text{ and } q_{\{i,j\},i} - \omega_i = \frac{\psi_i}{b_2} (\bar{p}_i - p_{\{i,j\}}).$$

- Linkage eliminates the post-shock wedge in autarkic prices
- ...and increases/decreases effective cap in high-/low-shock jurisdiction
- The expected aggregate economic benefit from  $\{i, j\}$ -linkage is

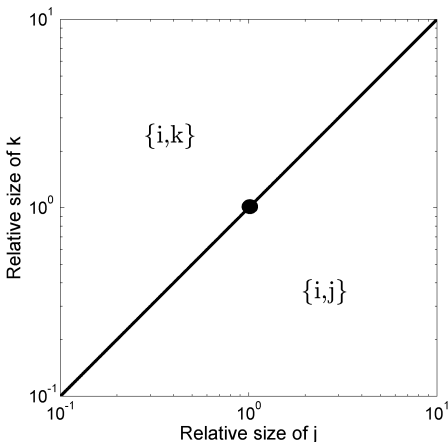
$$\mathbb{E}\{\Delta_{\{i,j\}}\} = \frac{\psi_i \psi_j}{2b_2 (\psi_i + \psi_j)} (\sigma_i^2 + \sigma_j^2 - 2\rho_{ij} \sigma_i \sigma_j) \geq 0,$$

- ...and is shared in inverse to proportion to size

$$\mathbb{E}\{\delta_{\{i,j\},i}\} / \mathbb{E}\{\delta_{\{i,j\},j}\} = \psi_j / \psi_i.$$

# Bilateral linkage preferences

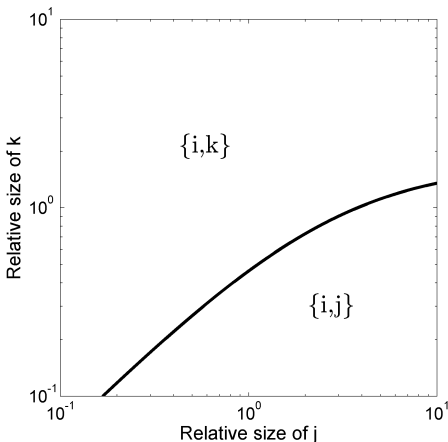
$i$ 's preferences over **bilateral linkages** in a 3-jurisdiction world



- $\{i, j, k\}$
- $\psi_i = 1$
- $\sigma_i = \sigma_j = \sigma_k$
- $\rho_{ij} = \rho_{ik}$

# Bilateral linkage preferences

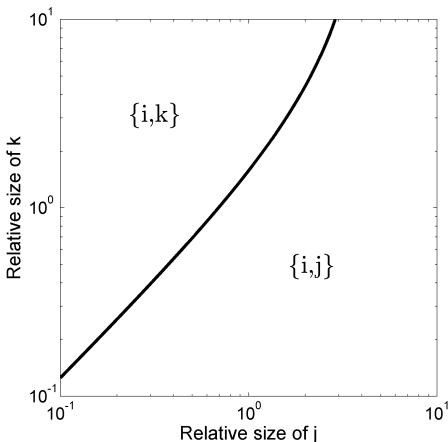
$i$ 's preferences over **bilateral linkages** in a 3-jurisdiction world



- $\{i, j, k\}$
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- $2\sigma_i = 2\sigma_j = \sigma_k$
- $\rho_{ij} = \rho_{ik} = 0$

# Bilateral linkage preferences

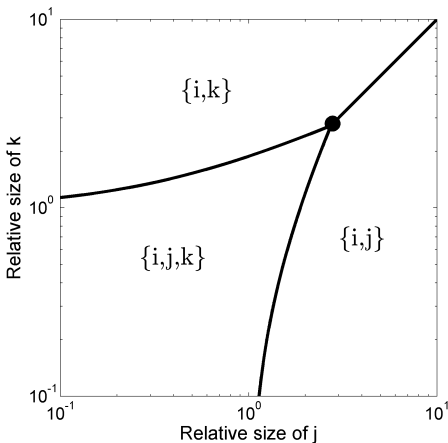
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- $\{i, j, k\}$
- $\psi_i = 1$
- $\sigma_i = \sigma_j = \sigma_k$
- $\rho_{ij} = -0.5, \quad \rho_{ik} = 0$

# Enter trilateral linkage

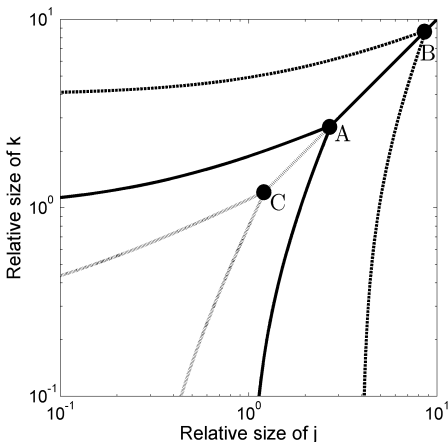
$i$ 's preferences over **all linkages** in a 3-jurisdiction world



- $\{i, j, k\}$
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# Enter trilateral linkage

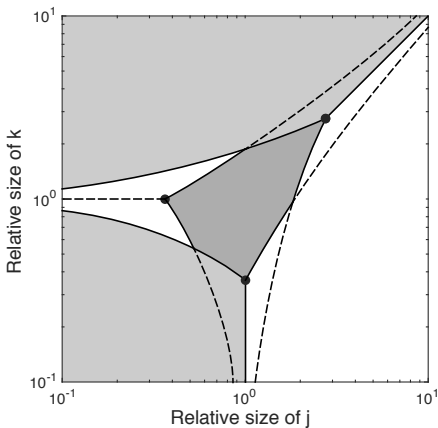
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- $\{i, j, k\}$
- $\psi_i = 1$
- $\rho_{ij} = \rho_{ik} = \rho_{jk} = 0$
- **A**:  $\sigma_i = \sigma_j = \sigma_k$
- **B**:  $\sigma_i = 2\sigma_j = 2\sigma_k$
- **C**:  $2\sigma_i = \sigma_j = \sigma_k$

# Enter trilateral linkage

## $i, j$ and $k$ 's preferences under symmetry



- $\{i, j, k\}$
- $\psi_i = 1$
- $\sigma_i = \sigma_j = \sigma_k$
- $\rho_{ij} = \rho_{ik} = \rho_{jk} = 0$
- symmetry



# Multilateral linkage equilibria

- A  $\mathcal{C}$ -linkage equilibrium is the  $(|\mathcal{C}| + 1)$ -tuple  $(p_{\mathcal{C}}, (q_{\mathcal{C},i})_{i \in \mathcal{C}})$  where

$$p_{\mathcal{C}} = \Psi_{\mathcal{C}}^{-1} \sum_{i \in \mathcal{C}} \psi_i \bar{p}_i, \text{ and } q_{\mathcal{C},i} - \omega_i = \frac{\psi_i}{b_2} (\bar{p}_i - p_{\mathcal{C}}).$$

- Under  $\mathcal{C}$ -linkage, the economic gain accruing to jurisdiction  $i \in \mathcal{C}$  is

$$\mathbb{E}\{\delta_{\mathcal{C},i}\} \propto \psi_i \mathbb{E}\{(\bar{p}_i - p_{\mathcal{C}})^2\} = \psi_i ((\mathbb{E}\{\bar{p}_i\} - \mathbb{E}\{p_{\mathcal{C}}\})^2 + \mathbb{V}\{\bar{p}_i - p_{\mathcal{C}}\}) \geq 0.$$

- Total gain in  $\mathcal{C}$ -linkage is **decomposed into its internal bilateral linkage gains**

$$\Delta_{\mathcal{C}} = \sum_{i \in \mathcal{C}} \delta_{\mathcal{C},i} = (2\Psi_{\mathcal{C}})^{-1} \sum_{(i,j) \in \mathcal{C}^2} (\psi_i + \psi_j) \Delta_{\{i,j\}}.$$

- Linking disjoint linkage coalitions is beneficial: **linkage is superadditive**
  - Jurisdictional linkage preferences are not aligned
  - Global market is not necessarily the most preferred link for all  $i \in \mathcal{I}$ .
  - Any linkage coalition different from the global market cannot be the most preferred linkage coalition for all coalition members.

# Calibration methodology and results

- Assume hypothetical ETS covering all emissions of CHN, USA, EUR, KOR, EGY: sample representative of diversity present in the data
- Calibrate  $\{\psi_i, \sigma_i, \rho_{ij}\}$  based on historical emissions data
- WRI: Annual country level CO<sub>2</sub> emissions data covering 1950-2012
- The natural logarithm of laissez-faire emissions is

$$\ln(\tilde{q}_i) = \ln(b_2/\psi_i) + \ln(b_1 + \theta_i)$$

- We associate each component of  $\ln(\tilde{q}_i)$  with the trend and cyclical components of emissions obtained using the HP filter with the penalty parameter  $\lambda = 6.25$  for annual data (Hodrick & Prescott, 1997)
- Congruent with assumption that shocks driven by business cycles, technology shocks, fuel prices,... See Doda (2014) for methodology and Doda & Taschini (2017) for discussion of results

# Calibration methodology and results

**Table:** Calibration results: Size and volatility ( $\psi_i$  and  $\sigma_i$ )

	CHN	USA	EUR	KOR	EGY
$\psi_i$	100	55.038	38.699	6.645	2.356
$\sigma_i$	0.028	0.019	0.017	0.034	0.050

**Table:** Calibration results: Pairwise correlation coefficients ( $\rho_{ij}$ )

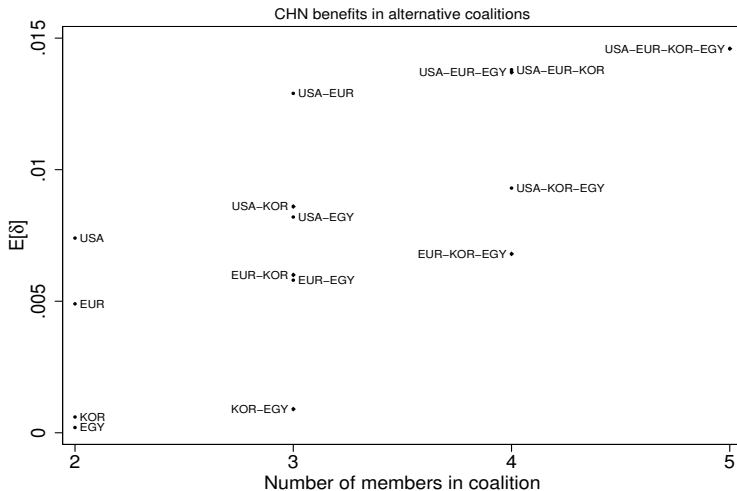
	CHN	USA	EUR	KOR	EGY
CHN	1.000				
USA	0.525	1.000			
EUR	0.460	0.652	1.000		
KOR	0.247	0.419	0.277	1.000	
EGY	-0.395	-0.186	-0.101	-0.397	1.000

# Most and second preferred coalitions

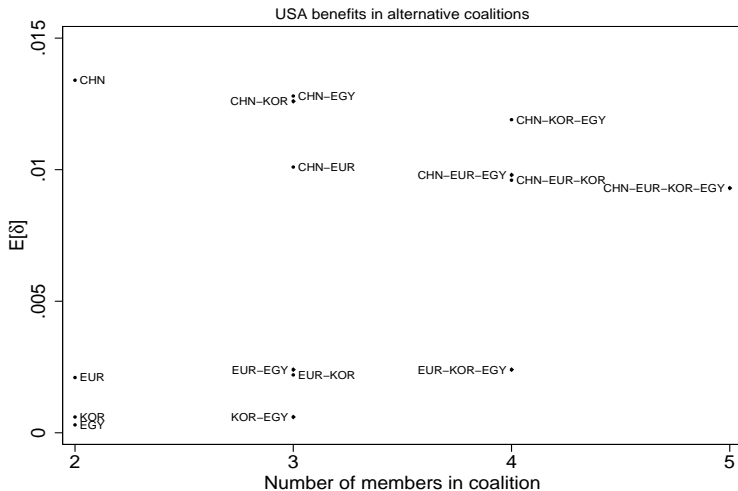
	Most preferred coalition	Second most preferred coalition
CHN	{CHN, USA, EUR, KOR, EGY}	{CHN, USA, EUR, KOR}
USA	{CHN, USA}	{CHN, USA, EGY}
EUR	{CHN, EUR}	{CHN, EUR, KOR, EGY}
KOR	{CHN, KOR}	{CHN, KOR, EGY}
EGY	{CHN, EGY}	{CHN, KOR, EGY}

- CHN ranks linkage coalitions by size
- Preferences of USA/EUR/KOR/EGY
  - Bilateral link with CHN is always top choice
  - Second preferences always include CHN but subtle otherwise
    - KOR prefers to link with EGY than with much larger USA or EUR

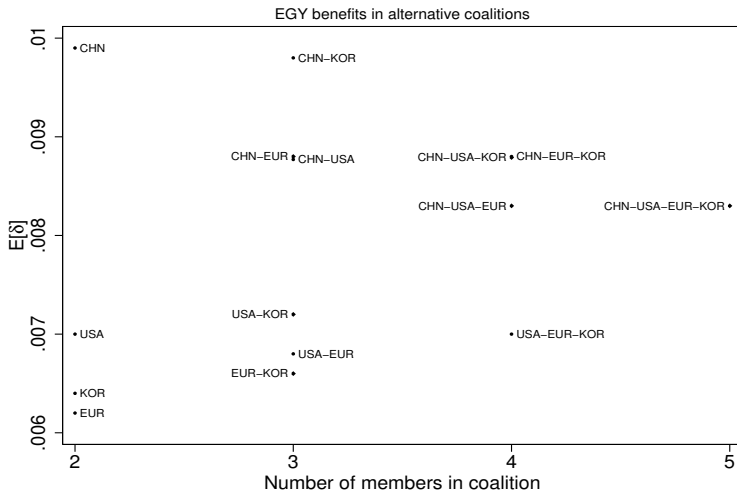
# CHN linkage gains



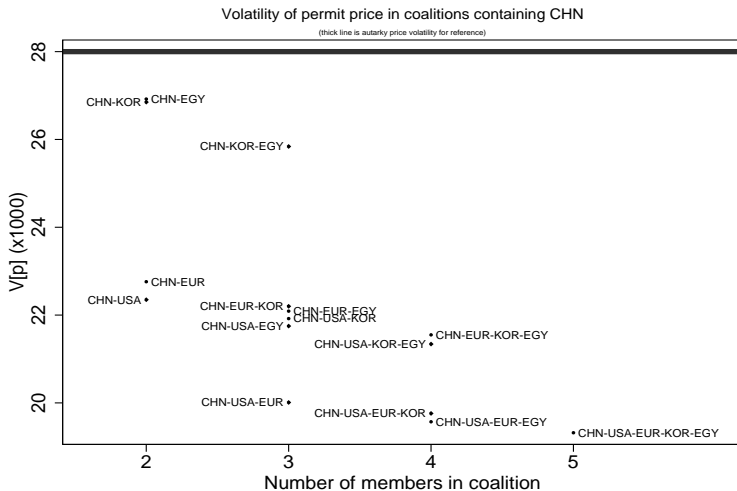
# USA linkage gains



# EGY linkage gains

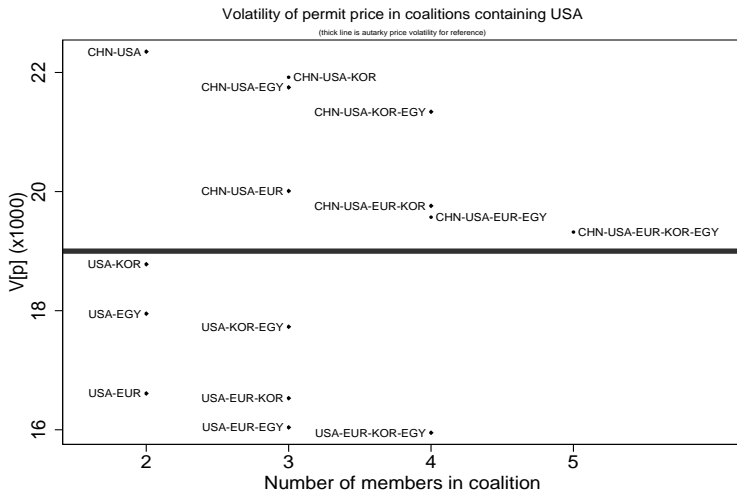


# CHN price volatility

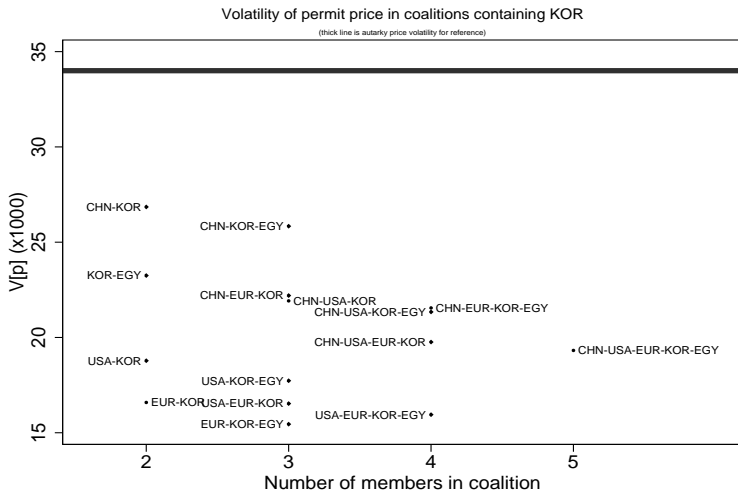




# USA price volatility



# KOR price volatility



# Linkage costs and cost-sharing arrangements

	$S^*$	$\mathbb{E}\{\bar{\Delta}_{S^*}\}$	Set of blocking jurisdiction under R#
$z = 0$	$\{\{\text{CHN, USA, EUR}\}, \{\text{KOR, EGY}\}\}$	0.0221	$R3$ and $R5$ : $\emptyset$ $R1, R2, R4, R6, R7, \dots$ $\dots R8$ and $R9$ : $\{\text{KOR}\}$
$z = 0.5$	$\{\{\text{CHN, USA, EUR}\}, \{\text{KOR, EGY}\}\}$	0.0137	$R1, R4, R5$ and $R7$ : $\emptyset$ $R2$ : $\{\text{KOR}\}$ $R3$ : $\{\text{EUR}\}$ $R6$ and $R8$ : $\{\text{EUR, KOR}\}$ $R9$ : $\{\text{CHN}\}$
$z = 1$	$\{\{\text{CHN, USA, EUR, KOR, EGY}\}\}$	0.0118	$R5$ : $\emptyset$ $R1$ : $\{\text{KOR}\}$ $R2$ and $R4$ : $\{\text{CHN, USA}\}$ $R3$ and $R6$ : $\{\text{KOR, EGY}\}$ $R7$ : $\{\text{CHN}\}$ $R8$ : $\{\text{USA, EUR}\}$ $R9$ : $\{\text{EGY}\}$

## Appendix of Chapter 3

# Motivation & Literature – Stylized Facts

- Under textbook assumptions: intertemporal cost efficiency
  - current price reflects NPV of last permit used (Rubin, 1996)
  - optimal price path grows at rate of interest (Hotelling, 1931)
  - focus on long-term carbon price signal
- Recurrent observations: prices lower than anticipated and formation of allowance surpluses (Tvinnereim, 2014)
  - cap erosion: crisis, offsets, CPs,... (Borenstein et al, 2016)
  - price determinants (Koch et al, 2014; Hintermann et al, 2016)
- The potential suspects are (non mutually exclusive):
  - myopia/limited foresight (Ellerman et al, 2016)
  - excessive discounting 1 (Neuhoff et al, 2012)
  - excessive discounting 2 (Bredin & Parsons, 2016)
  - excessive discounting 3 (Kollenberg & Taschini, 2016)
  - regulatory uncertainty (Salant, 2016; Koch et al, 2016)

# Motivation & Literature – Regulatory Uncertainty (RU)

- RU = individual's perceived inability to predict the future state of the regulatory environment (Hoffmann et al, 2008)
  - (deep) uncertainty in the sense of Knight (1921)
  - regulatory risks are not (entirely) hedgeable
  - political nature of permits = 'ill-defined' property rights
- RU undermines long-term credibility and affects current prices (Salant, 2016; Salant & Henderson, 1978)
  - EUETS reacts to political announcements (Koch et al, 2016)
- RU increases compliance costs by delaying investments
  - option value to postpone investments (Dixit & Pindyck, 1994)
  - empirical validation based on CAIR (Dorsey, 2017)
- We use a two-period model for an ambiguity-averse firm
  - to capture the influence of RU on abatement decisions
  - to find theoretical/behavioral foundations to observed facts
  - to analyze the impact of allocation on banking decisions

# Ambiguity Aversion (AA) and Representation Theorem

- Ambiguity = inability to unambiguously assign a probability measure uniquely describing the underlying risk
- Ambiguity aversion = additional aversion (w.r.t. risk aversion) to being unsure about the probabilities of outcomes
- Ample lab experiments: agents prefer gambles with known rather than unknown probabilities (and DAAA prevails)
- Firm exhibits smooth ambiguity aversion (KMM, 2005; 2009)
  - uncertain about the objective future price risk  $\tilde{r}$
  - confronted with objective risks  $\tilde{r}_\theta$  in scenarios  $\theta \in \Theta = [\underline{\theta}; \bar{\theta}]$
  - has subjective beliefs over  $\theta$ -scenarios  $F$
  - Ambiguity = subjective risk over objective risks, i.e. two layers of uncertainty:  $SEU \times \phi(EU)$  with  $\phi' > 0$  and  $\phi'' \leq 0$  (AA)

# Firm's Objective Function & Benchmark

- Two dates 1 and 2, uncertainty resolves at date 2
- for any given observed couple  $(\tau, \xi)$ , temporal profits write

$$\pi_1(a_1) = \zeta_1 - C_1(a_1) \text{ and } \pi_2(a_1, a_2) = \zeta_2 - C_2(a_1, a_2) - \tau(\xi - a_1 - a_2 - \omega).$$

- The firm trades off its present abatement cost with its future certainty-equivalent benefit of banking

$$\begin{aligned} \max_{a_1 \geq 0} \pi_1(a_1) + \beta \phi^{-1}(\mathbb{E}_F\{\phi(\mathcal{V}(a_1; \tilde{\theta}))\}), \\ \text{where } \mathcal{V}(a_1; \theta) = \mathbb{E}\{\pi_2(a_1, a_2^*(a_1, \omega; \tilde{\tau}_\theta); \tilde{\tau}_\theta) | \theta\}. \end{aligned} \quad (1)$$

- Program (1) is well defined for  $\pi_{1,2}$  and  $-\phi'/\phi''$  concave
- Benchmark = ambiguity neutrality ( $\phi$  linear). The FOC is

$$\pi_1'(\bar{a}_1) + \beta \mathbb{E}_F\{\mathcal{V}_{a_1}(\bar{a}_1; \tilde{\theta})\} = 0 \Leftrightarrow \pi_1'(\bar{a}_1) + \beta \mathbb{E}\{\tilde{\tau}\} = 0, \quad (2)$$

i.e. cost-efficiency obtains and  $\bar{a}_1$  independent of allocation  $\omega$ .



## Two Ambiguity Aversion Induced Effects (1/3)

- Under ambiguity aversion, FOC for Program (1) reads

$$\pi'_1(\hat{a}_1) + \beta \mathcal{A}(\hat{a}_1) \mathbb{E}_F \{ \mathcal{D}(\hat{a}_1; \tilde{\theta}) \mathcal{V}_{a_1}(\hat{a}_1; \tilde{\theta}) \} = 0, \text{ where} \quad (3)$$

- $\mathcal{A}$  modifies the subjective discount factor such that

$$\mathcal{A}(a_1) = \frac{\mathbb{E}_F \{ \phi'(\mathcal{V}(a_1; \tilde{\theta})) \}}{\phi' \circ \phi^{-1}(\mathbb{E}_F \{ \phi(\mathcal{V}(a_1; \tilde{\theta})) \})}, \quad (4)$$

and  $\mathcal{A} \geq, =, \leq 1$  i.f.f.  $\phi$  displays DAAA, CAAA, IAAA

- $\mathcal{D}$  pessimistically distorts the subjective prior  $F$  such that

$$\forall \theta \in \Theta, \mathcal{D}(a_1; \theta) = \frac{\phi'(\mathcal{V}(\bar{a}_1; \theta))}{\mathbb{E}_F \{ \phi'(\mathcal{V}(\bar{a}_1; \tilde{\theta})) \}}, \quad (5)$$

and overweights bad scenarios with low- $\mathcal{V}$  values ( $\phi'' \leq 0$ ).

## Two Ambiguity Aversion Induced Effects (2/3)

- Increase in banking under AA w.r.t. AN ( $\hat{a}_1 \geq \bar{a}_1$ ) i.f.f.

$$\mathcal{A}(\bar{a}_1) \mathbb{E}_H \{ \mathcal{V}_{a_1}(\bar{a}_1; \tilde{\theta}) \} \geq \mathbb{E}_F \{ \mathcal{V}_{a_1}(\bar{a}_1; \tilde{\theta}) \}, \quad (6)$$

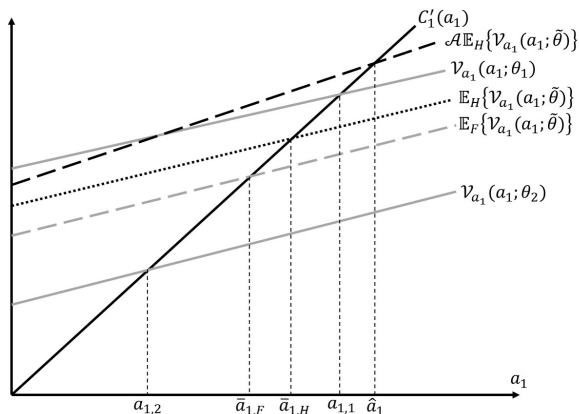
with  $H$  the distorted prior  $H(\theta) = \int_{\underline{\theta}}^{\theta} \mathcal{D}(\bar{a}_1; X) dF(X)$ , i.e. the future price estimate is higher under AA than AN

- Controlling for *pessimism* ( $H \equiv F$ ),  $\mathcal{A} \geq 1$  raises banking
  - DAAA  $\sim$  ambiguity prudence (Berger, 2014; Gierlinger & Gollier, 2017)
  - corresponds to an increase in firms' discount factor
  - ample evidence of DAAA in lab experiments and surveys
- Controlling for *prudence* ( $\mathcal{A} \equiv 1$ ), pessimism raises banking only if low- $\mathcal{V}$  scenarios coincide with high- $\mathcal{V}_{a_1}$  scenarios
- The two AA effects can be aligned or countervailing

## Two Ambiguity Aversion Induced Effects (3/3)

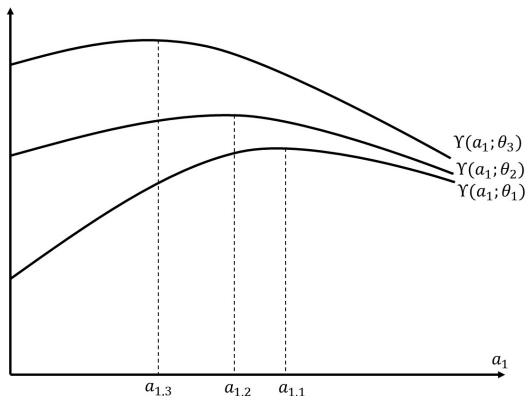
Illustration:  $\Theta = \{\theta_1; \theta_2\}$ ,  $F = \{\theta_1, .5; \theta_2, .5\}$ , both  $\mathcal{A}$  and  $\mathcal{D}$  are constant with  $a_1$ . Joint AA-effect is decomposed into two steps

$F \rightarrow H$  is a vertical translation;  $\mathcal{A}$  is rotation



# Characterization of pessimism (1/3)

- Pessimism raises banking i.f.f.  $\text{Cov}_\theta \{ \mathcal{V}(\bar{a}_1; \tilde{\theta}); \mathcal{V}_{a_1}(\bar{a}_1; \tilde{\theta}) \} \leq 0$
- Illustration:  $\Theta = \{ \theta_1; \theta_2; \theta_3 \}$ . Higher banking reduces the spread across scenarios under negative correlation



# Characterization of pessimism (2/3)

## Proposition: Sufficient conditions for over-banking

Pessimism leads the firm to over-abate at date 1 if:

- (i) they expect to be in a net short position at date 2 in all  $\theta$ -scenarios,
- (ii) or, their initial allocation is relatively small.

- Pessimism induces a precautionary effect
  - net buyers bank more to hedge against future price
- banking adjustment dictated by initial allocation
  - allocation is not neutral and determines bad/good scenarios

## Proposition: Ambiguity on individual baselines

Consider a continuum of competitive firms, identical but for allocation. Under symmetric allocation of allowances, firms always over-bank at date 1.

# Characterization of pessimism (3/3)

- Three extensions of the model:

## Proposition: Introduction of forwards contracts

Under the assumption that forwards contracts are fairly priced, intertemporal efficiency (in expectations) is restored under CAAA. However, forwards cannot correct for subjective shifts in discounting.

## Proposition: Market populated by both AA and AN firms

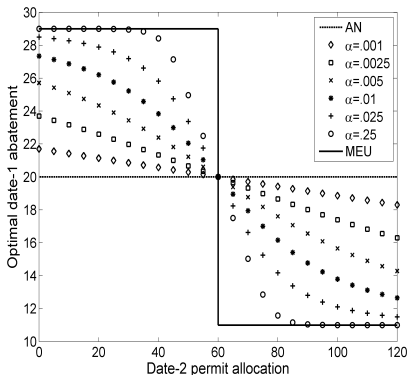
The AA-induced distortion is amplified in a market populated by a mix AA and AN firms. This also alters abatement decisions by AN firms.

## Proposition: Equilibrium volume of trade (autarkic compliance)

If permits are sufficiently non-symmetrically distributed across AA firms, then the equilibrium volume of trade is lower than with AN firms.

# Comparative statics and numerical simulations (1/3)

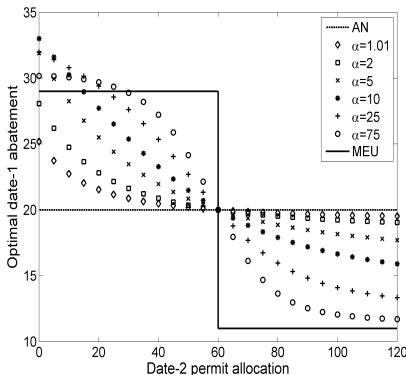
- An increase in AA ( $\phi_2 = \psi \circ \phi_1$ ,  $\psi' > 0$ ,  $\psi'' \leq 0$ ) leads to
  - an increase in pessimism (MLR deterioration; Gollier, 2011)
  - when  $\psi$  is almost quadratic, an increase in prudence only if prudence is not too high relative to AA  $-\phi_1''/\phi_1' \leq -\phi_1'''/\phi_1'' \leq -3\phi_1''/\phi_1'$
- With uniform measures and controlling for prudence (CAAA)



- banking decreases with  $\omega$
- unique crossing at  $\omega = 60$
- magnitude of variation increases with AA degree
- continuum between AN and the MEU criterion

# Comparative statics and numerical simulations (2/3)

- An increase in AA ( $\phi_2 = \psi \circ \phi_1$ ,  $\psi' > 0$ ,  $\psi'' \leq 0$ ) leads to
  - an increase in pessimism (MLR deterioration; Gollier, 2011)
  - when  $\psi$  is almost quadratic, an increase in prudence only if prudence is not too high relative to AA  $-\phi_1''/\phi_1' \leq -\phi_1'''/\phi_1'' \leq -3\phi_1''/\phi_1'$
- With uniform measures and accounting for prudence (DAAA)



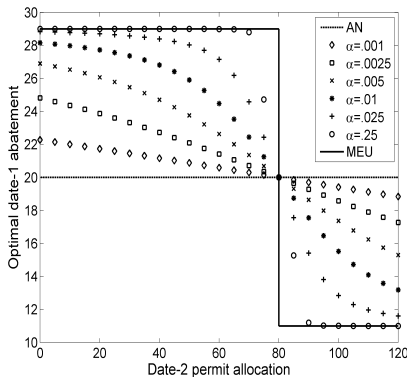
- upward offset due to  $\mathcal{A}$
- weak  $\mathcal{A}$ -effect for medium  $\omega$
- higher  $\mathcal{A}$ -effect for low  $\omega$  with multiple crossings
- MEU breach for low  $\omega$
- except for extreme  $\omega$ , banking is driven by pessimism



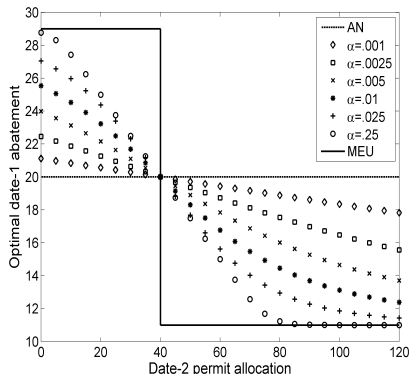
# Comparative statics and numerical simulations (3/3)

- Joint market price and individual baseline ambiguities
- With uniform probability measures and CAAA ( $G$  and  $L$  are first-order independent given any  $\theta$ -scenario  $\mathbb{E}_{\{G,L\}}\{\cdot|\theta\} \equiv \mathbb{E}_{\{G\}}\{\cdot|\theta\}\mathbb{E}_{\{L\}}\{\cdot|\theta\}$ )

$\text{Cov}_{\theta}\{G, L\} > 0$



$\text{Cov}_{\theta}\{G, L\} < 0$



# Overestimation of AA effects

- Marinacci (2015), Guetlein (2016), Bosetti & Berger (2017)
- Decomposition:  $\phi = v \circ u^{-1}$ ,  $u'' \leq 0$  denotes risk aversion and  $v'' \leq 0$  denotes aversion towards model uncertainty
- liable firms are risk-neutral but model-uncertainty averse

$$\frac{-\phi''}{\phi'} = \frac{1}{u'} \left( \frac{-v''}{v'} - \frac{-u''}{u'} \right)$$

- AA requires  $v$  being more concave than  $u$
- Amplification:  $\frac{-\phi''}{\phi'} \Big|_{RN} \geq \frac{-\phi''}{\phi'} \Big|_{RA}$

# Ambiguity premium

## Proposition: Sufficient condition for over-banking

Let liable firms display CAAA. Then, it is sufficient that  $(\mathcal{V}(\bar{a}_1; \theta))_\theta$  and  $(\mathcal{V}_{a_1}(\bar{a}_1; \theta))_\theta$  be anticomomonotononic for over-abatement to occur at date 1.

- For illustration, let  $\partial_{a_1} C_2 \equiv 0$ . Expanding the FOC gives

$$\hat{a}_1 \geq \bar{a}_1 \Leftrightarrow \begin{cases} \mathcal{A}(\bar{a}_1) (\langle \tilde{\tau} \rangle + \mathcal{P}(\bar{a}_1)) \geq \langle \tilde{\tau} \rangle, \\ \mathcal{P}(a_1) = \frac{\text{Cov}\{\phi'(\mathcal{V}(a_1; \tilde{\theta})); \mathcal{V}_{a_1}(a_1; \tilde{\theta})\}}{\mathbb{E}_F\{\phi'(\mathcal{V}(a_1; \tilde{\theta}))\}} \end{cases}$$

- $\mathcal{P}$  is an ambiguity premium demanded to compensate the exposure to ambiguity, which is positive provided that anticomomonotonicity holds

## Proposition: Necessary and sufficient conditions

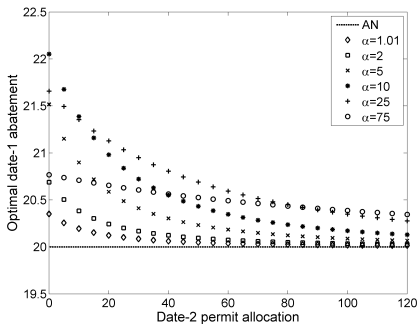
$\hat{a}_1 \geq \bar{a}_1$  i.f.f.  $\mathcal{P}(\bar{a}_1) \geq 0$  under CAAA, or  $\mathcal{P}(\bar{a}_1) \geq \frac{1 - \mathcal{A}(\bar{a}_1)}{\mathcal{A}(\bar{a}_1)} < 0$  under DAAA.

# Parametrical example (1/7)

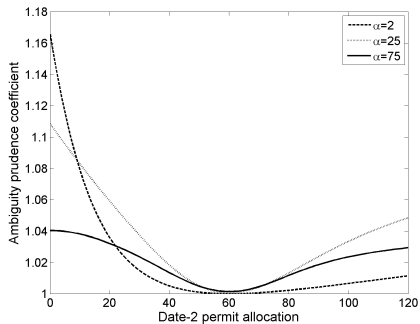
- $c_1 = c_2 = 1$ ,  $\beta = 1$  and  $\gamma = 0$
- $F \hookrightarrow \mathcal{U}(\Theta = \llbracket -\bar{\theta}; \bar{\theta} \rrbracket)$ , with  $\bar{\theta} = 9$
- Under a cap and trade with fixed common baselines  $\xi = 100$ 
  - $G(\cdot; \theta) \hookrightarrow \mathcal{U}(\llbracket \underline{\tau} + \theta; \bar{\tau} + \theta \rrbracket)$ , with  $\underline{\tau} = 10$  and  $\bar{\tau} = 30$
  - $\mathcal{V}_{a_1}(a_1; \theta) = \langle \tau \rangle + \theta$  with  $\langle \tau \rangle = \frac{\underline{\tau} + \bar{\tau}}{2}$
  - $\Rightarrow$  under AN  $\langle \tilde{\tau} \rangle = \langle \tau \rangle = 20$
  - AntiC holds given that  $\omega \leq \omega^* = 51$  with  $\omega \in [0; 120]$
- Under a tax regime with  $t = 20$  for consistency
  - $G(\cdot; \theta) \hookrightarrow \mathcal{U}(\llbracket \underline{\xi} + \theta; \bar{\xi} + \theta \rrbracket)$ , with  $\underline{\xi} = 50$  and  $\bar{\xi} = 150$
  - Liability thresholds: tax charged only above  $\omega \in [0; 120]$
- The ambiguity function  $\phi$  is such that
  - CAAA:  $\phi(x) = \frac{e^{-\alpha x}}{-\alpha}$  with  $\alpha > 0$  the AAA degree
  - DAAA:  $\phi(x) = \frac{x^{1-\alpha}}{1-\alpha}$  with  $\alpha > 1$  the AAA degree

# Parametrical example (2/7)

Tax only subject to  $\mathcal{A}$

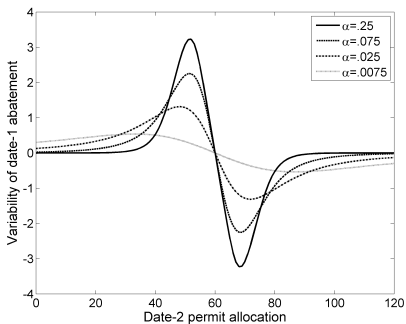


$\mathcal{A}$ -effect in an ETS

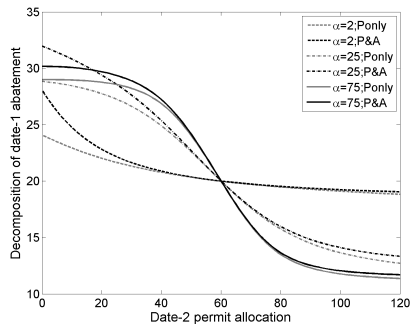


# Parametrical example (3/7)

## Variability under CAAA



## Decomposition of $\mathcal{A}$ and $\mathcal{P}$



# Parametrical example (4/7)

Illustration: Let  $\Theta = \{\theta_1 = +5; \theta_2 = -5\}$ ,  $F = \{\theta_1, .5; \theta_2, .5\}$ . FOCs and the decomposition are given by

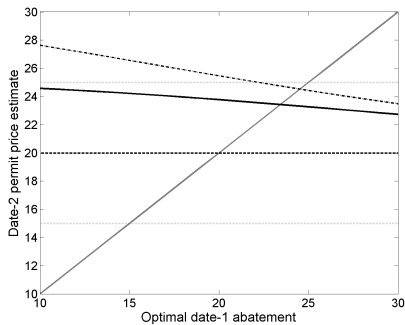
$$-C'_1(\hat{a}_1) + \beta \mathcal{A}(\hat{a}_1) (\langle \tau \rangle + \hat{q}_1(\hat{a}_1)\theta_1 + \hat{q}_2(\hat{a}_1)\theta_2) = 0 \quad (7)$$

$$H(a_1) = \begin{cases} \hat{q}_1(a_1) = q_1 \frac{\phi'(\mathcal{V}(a_1; \theta_1))}{q_1 \phi'(\mathcal{V}(a_1; \theta_1)) + q_2 \phi'(\mathcal{V}(a_1; \theta_2))} \\ \hat{q}_2(a_1) = q_2 \frac{\phi'(\mathcal{V}(a_1; \theta_2))}{q_1 \phi'(\mathcal{V}(a_1; \theta_1)) + q_2 \phi'(\mathcal{V}(a_1; \theta_2))} \end{cases} \quad (8)$$

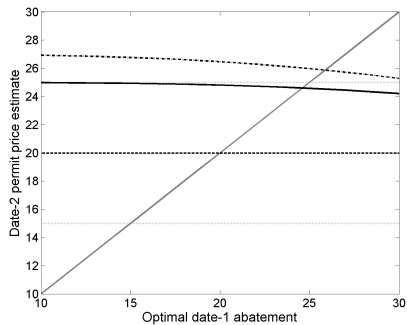
$$\mathcal{A}(a_1) = \frac{q_1 \phi'(\mathcal{V}(a_1; \theta_1)) + q_2 \phi'(\mathcal{V}(a_1; \theta_2))}{\phi' \circ \phi^{-1}(q_1 \phi(\mathcal{V}(a_1; \theta_1)) + q_2 \phi(\mathcal{V}(a_1; \theta_2)))} \quad (9)$$

# Parametrical example (5/7)

$$\alpha = 5 \ \& \ \omega = 20$$



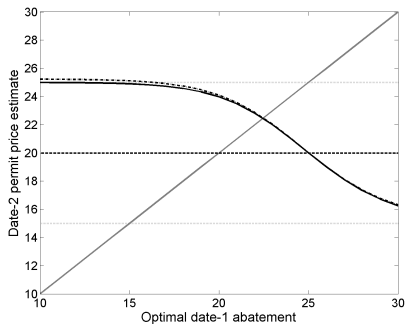
$$\alpha = 10 \ \& \ \omega = 20$$



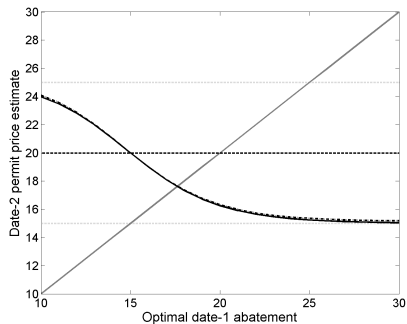


# Parametrical example (6/7)

$$\alpha = 75 \text{ \& \; } \omega = 55$$

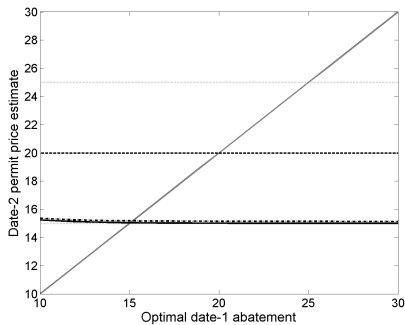


$$\alpha = 75 \text{ \& \; } \omega = 65$$



# Parametrical example (7/7)

$$\alpha = 75 \text{ \& } \omega = 80$$



$$\alpha = 5 \text{ \& } \omega = 90$$

